Crossover ii¹ Patrick D. Elliott & Martin Hackl April 2, 2020

Tentative revised schedule

We'll make an announcement on Friday about how the class will look for the rest of the semester, but the tentative plan is to spend a little bit more time talking about crossover, before moving on to presupposition and Haddock's puzzle.

N.b. we skipped class in the first week of March, as I was away at a conference. This still needs to be rescheduled – we'll be in touch about possible dates.

Projects

Registered students: thanks for submitting your project proposals. If you haven't already done so, please get in touch with either me, Martin (or both of us!) to arrange a time to talk through your proposal.

1 Last time – Barker & Shan: wco as a reflex of evaluation order

At the beginning of the semester, we learned about a theory of scope-taking with a built-in left-to-right bias – *continuation semantics*.

Concretely, due to the way that the composition rule Scopal Function Application (SFA) was defined, evaluation of quantificational effects *mirrors* linear order.²

(1) Scopal Function Application (SFA) (def.)

$$\frac{f[]}{x} \operatorname{S} \frac{g[]}{y} \coloneqq \frac{f[g[]]}{x \operatorname{A} y}$$

As we saw in the last class, an appealing consequence of this linear bias was a natural account of Weak Crossover (wco) in terms of evaluation order.³

Recall, a simplified version of the wco paradigm: scope can feed binding (2), unless the binder doesn't precede the bound expression (3).⁴

² To cash this out, we needed to say something concrete about the syntax-semantics interface – concretely, we committed to the ideas that (a) the basic combinatoric operation MERGE is asymmetric, and (b) the syntactic and semantic composition proceed in lockstep (direct compositionality; Jacobson 1999, 2014).

³ See especially Shan & Barker 2006 and Barker & Shan 2014: chapters 2 and 4.

⁴ Throughout, i'll use superscript indices to indicate the binder, and subscript indices to indicate the bound expression(s).

¹ 24.979: Topics in semantics *Getting high: Scope, projection, and evaluation order*

- (2) [Everyone^x's mother] bought them_x a bicycle.
- Their_x mother showered everyone^x with gifts.
 cf. a different person showered everyone with gifts.

The idea, briefly, was to generalize our notion of a scope-taker to make sense of the idea that pronouns also *scope*.

In Barker & Shan's system, pronouns take scope in the following way: they expect *a proposition*, and they return an *open proposition*.⁵

In order for a Quantificational Phrase (QP) to bind a pronoun, it must first be *bind-shifted*. A bind-shifted QP expects an open proposition, and returns a proposition. Successful binding is illustrated in figure 1.

⁵ We can helpfully think of an open proposition in this framework as a proposition with anaphoric effects (i.e., environment sensitivity).

Figure 1: Successful binding



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Putting mechanisms for inverse scope to one side, wco follows straightforwardly from this system. Since both pronouns and bind-shifted QPS are scopetakers, for the pronoun to be bound, the QP has to be evaluated first. Scope can feed binding, but the QP must precede the pronoun, since *evaluation order mirrors linear order*.⁶

Continuation semantics includes mechanisms for subverting the linear bias (namely, higher-order continuations), in order to account for inverse scope.

With mechanisms for inverse scope in the picture, things become a little less neat. Barker & Shan (2014) must stipulate that *lower* – the operation via which

⁶ One of the virtues of continuation semantics is that it straightforwardly accounts for scope out of Determiner Phrase (DP) without requiring *movement* out of DP. continuized meaning are collapsed into ordinary meanings – is rigidly typed. If we assume that *internal lower* is derived as lifted *lower*, this also has consequences for the type of internal lower:

Figure 2: Unsuccessful binding (wco)

This move basically guarantees, via a syntactic stipulation, that in order for a bind-shifted QP to bind a pronoun, it must take scope at the same tower-story as the pronoun. If it takes scope on a high level, then the resulting meaning cannot ultimately be lowered by a rigidly typed *lower*.

An unsuccessful attempt at getting internal lift to feed binding is illustrated in figure 2.

What's crucial here is that both lower and internal lower are rigidly typed.

Just how satisfying is this as an explanation though? If we look at what lower actually *does*, there's no intrinsic reason why it should be so rigidly typed.

As shown in (4), all that lower does is feed its sole argument the identity function. On a maximally polymorphic definition, therefore, the argument need only be of type $(a \rightarrow a) \rightarrow b$.

(4) Lower (maximally polymorphic ver.)
 m[↓] := *m* id

A maximally polymorphic lower could save the wco-violating derivation in figure 2.

Based on what lower *does*, there's no strong *semantic* motivation for making it rigidly typed. Therefore, despite the initial conceptual appeal of Barker & Shan's system, its success ultimately rests on what looks like a syntactic stipulation.

Maybe we can do better. One recent attempt to derive wco from independently motivated semantic mechanisms is Chierchia's *dynamic* account of wco.

Chierchia's account bears a family resemblance to that of Barker & Shan. It too attempts to derive wco from a semantic theory with a built-in left-to-right bias.



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- 2 Chierchia: wco as a reflex of the dynamics of anaphora

Chierchia (2020) develops a theory of wco based on dynamic semantics.

Much like continuation semantics, Dynamic Semantics (DS) is a semantic theory with a "built-in" left-to-right bias.

2.1 Dynamic semantics

Ds is one of the most empirically successful theories of anaphora (Heim 1982, Groenendijk & Stokhof 1991, Dekker 1994, a.o.) and presupposition projection (Heim 1983, Beaver 2001, a.o.). It has also been extended to a variety of other phenomena, including epistemic modality, exhaustification, and more.

Crowning achievements of Ds include analyses of the following phenomena:⁷

- Presupposition projection.⁸
- (5) a. [Ka visited Rome last summer]^{α}, and [she visited Rome again]_{α} this summer.
 - b. #[Ka visited Rome again]_α,
 and [she visited Rome last summer]^α.
- Donkey anaphora.
- (6) a. Every farmer who owns a donkey³ treasures it₃.
 b. ?Every farmer who owns it₃ treasures a donkey³.
- Cross-sentential anaphora.
- (7) a. A man¹ walked in. He₁ sat down.
 b. *He₁ sat down. A man₁ walked in.

Dwelling on cross-sentential anaphora, the contrast in (7) is clearly reminiscent of a wco effect.

As we'll see, orthodox dynamic semantics doesn't by itself explain wco, once quantificational scope is in the picture (see Charlow 2019 for discussion of this point), but Chierchia's basic intuition is to build a theory of wco based on this contrast.

In the next section, we'll introduce dynamic semantics by constructing an orthodox fragment that can account for cross-sentential anaphora. We'll move on ⁷ The (b) examples are included to briefly show that the phenomena under consideration exhibit a *left-to-right asymmetry*, thus motivating a dynamic treatment.

⁸ Approaches to dynamic semantics are split as to whether they collapse presupposition satisfaction and anaphora resolution (see, e.g., van der Sandt 1992) or not (Heim 1983).

The dynamic semantics ultimately adopted by Chierchia follows the latter tradition. This won't be so important for the purposes of this class, but will be relevant when we talk about presupposition, starting from next week! to show how it fails to capture wco, before moving on to Chierchia's modification.

2.2 A Heimian fragment

Sentential meanings in DS (Heim 1982, Groenendijk & Stokhof 1991, Chierchia 1995), have two essential components:

- An input-output asymmetry sentences denote *instructions* to change the input context (see especially Heim 1982).
- Indeterminacy certain expressions may induce an *indeterminate* output; an input can potentially be mapped to multiple outputs.

To model this formally, many theories of DS model sentence meanings as *relations between assignments* (equivalently: functions from assignments, to sets of assignments).⁹

DPS introduce Discourse Referents (DRS), modeled as variables; indefinites, unlike definites induce *indeterminacy*, concerning the identity of the DR. This is illustrated schematically in figure $3.^{10}$



Assignments are functions from variables to individuals; as is standard, we'll represent the set of variables as \mathbb{N} :¹¹

(8) Type of assignments $o := n \rightarrow e$

Chierchia assumes that assignments are *partial* functions.¹² That is to say, an assignment may only be defined for certain indices. The following are all valid assignments:

$$\begin{bmatrix} 1 \mapsto \text{roger} \\ 3 \mapsto \text{martin} \end{bmatrix} \qquad \begin{bmatrix} 4 \mapsto \text{kai} \\ 5 \mapsto \text{athulya} \\ 7 \mapsto \text{sabine} \end{bmatrix}$$

⁹ In actual fact, worlds need to enter the picture too – Heim (1982) models sentence meanings as relations between *assignment-world pairs*. This is independently necessary in order to account for the presupposition projection facts. Since we'll only be looking at the dynamic account of anaphora resolution, it will be harmless to ignore this aspect of the theory.

¹⁰ One way of thinking about this: definites induce a *functional* relation between assignments – every input assignment is mapped to a unique output assignment, whereas indefinites induce a *non-functional* relation between assignments – each input assignment can mapped to one or more output assignments.

Figure 3: Relations between assignments

¹¹ We'll use o as the type of assignments to distinguish between assignments used in a static setting.

¹² See also Rothschild & Mandelkern (2017) for a DS using partial assignments.

In order to characterize a dynamic sentential meaning, we define a type constructor T to abbreviate relations between assignments:

(9) Type of Context Change Potentials (CCPS) $T := o \rightarrow o \rightarrow t$

Here are some example sentence meanings:

Definites induce deterministic updates.

(10)
$$[Roger^1 \text{ arrived late}] = \lambda \omega \omega' \cdot \omega \stackrel{1/roger}{=} \omega' \wedge \text{arrived-late roger}^{13}$$

Indefinites induce non-deterministic updates:

(11) [[A linguist¹ arrived late]] =
$$\lambda\omega\omega'$$
. $\exists x [\omega \stackrel{1/x}{=} \omega' \land \text{arrived-late } x]$

We can get back an "ordinary" sentential meaning from a CCP by existentially closing the output assignment, as defined in (12).

(12) Dynamic closure (def.) $m^{\downarrow} := \lambda \omega . \exists \omega' [m \ \omega \ \omega']$ $\downarrow : T \rightarrow o \rightarrow t$

If we apply dynamic closure to a non-deterministic update, we get classical, existential truth-conditions; it will return true for any input assignment ω just in case *a linguist arrived late*.

How do we build up CCPs compositionally? Chierchia assumes that predicates are fundamentally Montagovian (i.e., functions of type $e \rightarrow t$):

(13) $[swim] := \lambda x \cdot swim x$ $e \to t$

Predicates are lifted into a dynamic setting by a type-shifter *dynamic lift*; d-lift takes a function from an individual to a truth-value, and shifts it into a function from an individual to a CCP – specifically, a dynamic *test*.¹⁴

(16) Dynamic lift (def.)

$$f^{\Delta} \coloneqq \lambda x \cdot \lambda \omega \cdot \lambda \omega' \cdot \omega = \omega' \wedge f x$$
 $\Delta \colon (e \to t) \to e \to T$

¹³ $\omega \stackrel{n/x}{=} \omega'$ is defined iff ω_n is *un*defined, and is true just in case ω' differs from ω at most in what *n* is mapped to.

Heim's *novelty condition* is essentially built into the rule for DR introduction.

Figure 4: Deterministic update

Т

Т



Figure 5: Non-deterministic update

$$\omega$$
A linguist¹ arrived late
$$\omega^{[1\mapsto kai]} \omega^{[1\mapsto roger]} \omega^{[1\mapsto sabine]}$$

¹⁴ A different way of generalizing this to n-place predicates is by giving Δ the following definition:

(14) $m^{\Delta} \coloneqq \lambda k \cdot \lambda \omega \omega' \cdot \omega = \omega' \wedge m k$ $\Delta : ((a \to t) \to t) \to (a \to t) \to t$

Chierchia's d-lift can be derived as follows, using the (by now very familiar) continuation semantics operations:

(15)
$$\lambda x . (x^{\uparrow} \mathsf{S} f^{\Delta \circ \uparrow})^{\downarrow}$$

Exercise

Chierchia defines dynamic lift in such a way that it only can apply to one-place predicates. This is not insignificant – see the discussion of event semantics later on. It is however trivial to generalize to d-lift to n-place predicates.

Generalize *dynamic lift* to *n*-place predicates by giving a recursive definition a la Partee & Rooth 1983.

Tests don't do anything interesting to input contexts. If we d-lift *swims* and apply it to *John* we'll get back a test that relates the input context ω to itself, iff *John swims* is true.

In orthodox dynamic fragments, all of the interesting dynamic action is triggered by arguments – specifically, pronouns and indefinites.

A pronoun indexed *n* expects a dynamic predicate *k* as its input, and returns a CCP – a function from an input assignment ω to the result of feeding ω_n into *k*, *re*-saturated with ω .¹⁵

(20) Pronouns (def.) $\text{pro}_n \coloneqq \lambda k \cdot \lambda \omega \cdot k \omega_n \omega^{16}$

Pronouns now may compose with d-lifted predicates via Function Application (FA), as illustrated in figure 6:



The result is a dynamic *test*, that saturates the argument of *swim* with whatever the input assignment ω maps to pronominal index 3 to.

In an orthodox dynamic fragment (Heim 1982, Groenendijk & Stokhof 1991), indefinites introduce DRS.¹⁷

(21) Indefinites (Heimian def.) someone_n := $\lambda k \cdot \lambda \omega \omega' \cdot \exists x, w'' [\omega \stackrel{n/x}{=} \omega'' \wedge k x \omega'' \omega']$

someone_n ($e \rightarrow T$) $\rightarrow T$

 $\text{pro}_n : (e \to T) \to T$

¹⁵ The type signature of a pronoun betrays the fact that, in this dynamic grammar, pronouns are *scope-takers*, and in fact, we can abbreviate a pronominal meaning using tower notation:

(17) Pronouns (tower def.) $\operatorname{pro}_{n} \coloneqq \frac{\lambda \omega . ([] \omega)}{\omega_{n}}$

Interestingly, this is what we get if we apply the *bind* of the Reader monad to the static entry for a pronoun.

- (18) Pronoun (static def.) pro_n := $\lambda \omega . \omega_n$
- (19) Bind of Reader (def.) $m^* \coloneqq \lambda k . \lambda \omega . k (m \omega) \omega$ $(o \rightarrow a) \rightarrow (a \rightarrow o \rightarrow b) \rightarrow o \rightarrow b$

 $o \rightarrow e$

¹⁶ Chierchia actually posits a syncategorematic rule for composing pronouns and dynamic predicates – instead, I've built what Chierchia's rule does into the meaning of the pronoun.

Figure 6: Pronouns in a dynamic fragment "He₃ swims"

¹⁷ Chierchia will ultimately reject this assumption, but it will be useful to consider his claims in light of the standard theory. In figure 7, we show how a Heimian indefinite composes in a dynamic fragment. The result maps each input assignment ω to (the characteristic function of) a *set* of assignments ω' , s.t., ω'_n is a swimmer.



Figure 7: Heimian indefinites in a dynamic fragment "Someone₇ swims"

A famous design feature of DS is an account of cross-sentential binding, as in the following famous examples:

(22) a. Someone¹ walked in and he₁ sat down.
b. Someone¹ walked in. he₁ sat down.

In DS, conjunction – as in (22a) – is treated as a special case of *discourse sequencing* (22b).

Discourse sequencing is an operation on CCPS:

(23) Dynamic sequencing (def.)

$$m; n \coloneqq \lambda \omega \cdot \lambda \omega' \cdot \exists \omega'' [m \omega \omega'' \wedge n \omega'' \omega']$$
 (;) : $T \to T \to T$

An illustration of how cross-sentential anaphora works in a Heimian fragment is given in figure 8: sequencing the CCPs gives rise to a CCP that relates ω and ω' just in case ω_4 is undefined and and ω'_4 walked in and sat down.



Why is DS promising as a starting point for a theory of wco? Recall the contrast below, reminiscent of wco: (24) a. Someone⁴ walked in and he sat down.
b. *He₄ walked in and someone⁴ sat down.

Just so long as *someone* takes scope within its containing sentence, DS captures this contrast, by virtue of the left-to-right bias built into the definition of discourse sequencing.

If we try to compute the CCP for (24b), the result is guaranteed to be undefined. This is because, if the input assignment ω is defined for 4, it can't also be *undefined* for 4, as is required by the meaning contributed by the indefinite.

(25) $\lambda\omega\omega'$. $\exists\omega''[\omega = \omega'' \land \text{sat-down } \omega_4 \land (\exists x[\omega'' \stackrel{4/x}{=} \omega' \land \text{walked-in } x])]$

Ds doesn't by itself however capture wco – this is because, independently, we need a mechanism that allows indefinites to *take scope*; indefinites introduce discourse referents at their scope site. We can therefore compute a bound reading for the following example, by scoping the indefinite over the pronoun:



Figure 9: Violating wco in a Heimian fragment "He₄ wants to meet someone⁴"

Intuitively, a problematic feature of DS in this regard is that it ties together DR introduction with quantificational scope.

2.3 The Dynamic Prediction Principle

At the heart of Chierchia account of wco is an apparently minor modification to orthodox dynamics, with far reaching consequences: the Dynamic Predication Principle (DPP), stated in (26).

(26) The Dynamic Predication Principle (DPP)DRS can only be introduced by predicates. (Chierchia 2020: p. 32)

Chierchia's innovation is to posit a second way of lifting predicates into a dynamic setting: *DR-lifting*.¹⁸

(27) DR-lift (def.) $f^{\Delta_n} := \lambda x \cdot \lambda \omega \cdot \lambda \omega' \omega \stackrel{n/x}{=} \omega' \wedge f x$ $\Delta_n : (e \to t) \to e \to T$ ¹⁸ If you try to generalize DR-lift to *n*-place predicates, you'll find that it can't be done in quite the same way as for d-lift. As an exercise, try to figure out why this.

Introducing DRs then, is no longer the job of *indefinites*, but rather the job of a DR-lifted predicate.

What do indefinites do then? For Chierchia, they're just type-lifted first-order quantifiers.¹⁹

(28) Dynamic existential quantification (def.) someone_n $m := \lambda \omega \omega' \cdot \exists x_n [m \omega \omega']$ someone_n : $T \to T$ ¹⁹ Looking at the definition in (28), you may be wondering how *someone* binds its trace. Chierchia does something rather sneaky here, which will be important later. For now, assume that it just works.

Someone saturates the argument that a DR was introduced relative to, and crosssentential anaphora proceeds as usual.



So far, we've constructed a system which replicates the basic results of orthodox dynamic semantics, but with a different compositional regime.

2.4 Accessibility

In the previous section, we only gave definitions for *dynamic conjunction/discourse sequencing* and the static first order existential.

Chierchia adopts the standard dynamic definitions for the other logical operators.

Negation is taken to be *externally static*; any DRs introduced in the scope of negation are subsequently wiped out.

(29) Dynamic negation (def.) $\neg m := \lambda \omega . \lambda \omega' . \omega = \omega' \land \neg (m^{\downarrow} \omega)$ $\neg : T \rightarrow T$

Externally static negation predicts the impossibility of binding in the following:²⁰

(31) *It's not the case that anyone¹ walked in. He₁ sat down.

To see why, first consider the prejacent of negation, with DR-lift applied to the predicate:²¹

(32) [anyone walked in]] =
$$\lambda \omega \omega'$$
. $\exists x [\omega \stackrel{1/x}{=} \omega' \land walked in x]$

Applying dynamic negation to the above CCP *existentially closes* the output assignment, thereby rendering it dynamically inert. The resulting CCP is a dynamic test, and asserts that there is no way of extending the input assignment s.t. 1 is mapped to someone who walked in (in other words, nobody walked in).

(33) \neg (32) = $\lambda\omega\omega'$. $\omega = \omega' \land \neg \exists \omega'', x[\omega \stackrel{1/x}{=} \omega'' \land walked-in x]$

Sequencing this CCP with the second conjunct will clearly not give rise to anaphora.

The remainder of the logical operations can be defined via first-order equivalent via dynamic conjunction, negation, and existential quantification. All are defined as operations on CCPS.

 (\rightarrow) : T \rightarrow T \rightarrow T

(34) Dynamic implication (def.)
$$m \rightarrow n \coloneqq \neg (m; \neg n)$$

²⁰ You might wonder about what we predict for a sentence such as the following, where the indefinite takes wide scope over negation:

(30) It's not true that someone walked in. He sat down.

This will be important later.

²¹ We simplify here and assume that Negative Polarity Item (NPI) *any* is just an existential licensed in the scope of negation.

- (35) Dynamic disjunction (def.) $m \lor n \coloneqq \neg (\neg m; \neg n)$ (\lor) : $T \to T \to T$
- (36) Dynamic universal quantifier (def.) everyone_n $m \coloneqq \neg \exists x_n (\neg m)$ $T \rightarrow T$

Famously, this way of dynamicizing the logical connectives gives rise to the following accessibility hierarchy in complex sentences:

(37) Accessibility (def.)A is *accessible* to B if a DR active in A can covary with a pronoun in B.

Accessibility in conjunctive sentences: [A and B]_S

- A is accessible to B (but not vice versa).
- B is accessible to whatever is conjoined with S.

(38) A man¹ walked in, and he₁ sat down. He₁ stood up again soon after.

Accessibility in conditional sentences: [if A then B]_S

- A is accessible to B (but not vice versa).
- A, B are *not* accessible to what is conjoined with S.²²

(39) #If someone¹ won the lottery, they₁ became rich. I shook their₁ hand.

Accessibility in negative sentences: [not A]_S

- Nothing in A is accessible to what is conjoined with S.
- (40) *It's not the case that anyone¹ sat down. He₁ walked in.

Accessibility in disjunctive sentences: [A or B]_S

• A is not accessible to B, nor is B to A.

²² In dynamic semantics, conditional sentences are internally dynamic, but externally static. • Neither A not B is accessible to what is conjoined with S.²³

(41) #Either Mary has a new dog¹, or I petted it₁.

2.5 Enter events

So far, we've constructed a fragment that only accommodates one-place predicates. This is actually by design – Chierchia argues that such a system has a natural bed-fellow in neo-Davisonian event semantics.²⁴

Traditions in event semantics:²⁵

Davidsonian:

(42) $[love] := \lambda exy \cdot exp = y \wedge th = x \wedge love e$ $v \to e \to e \to t$

Neo-Davidsonian (Castañeda 1967, Parsons 1990):

$$(43) \quad [love] := \lambda e \ . \ love \ e \qquad \qquad \lor \rightarrow$$

According to the neo-Davidsonian approach, all arguments are severed, and instead introduced by thematic role heads (the compositional regime adopted here is after Champollion 2015):²⁶

Thematic role heads take individuals and return properties of events – THEME returns a function from *x* to events of which *x* is the *theme*.

(44) THEME := $\lambda x \cdot \lambda e \cdot \text{th } e = x$ $e \to v \to t$

Abstracting away from dynamics for a moment, the composition of a simple sentence in a neo-Davidsonian setting can proceed via Predicate Modification (PM):

Note that, since verbs denote one place predicates, they can be DR-lifted.

Since the event argument of a verb is (by stipulation) existentially closed, this accounts for the possibility of eventive DRS, as in the following example:

(45) It rained⁴. It₄ was heavy.

 $^{\rm 24}$ We'll take the type of an event to be v.

²³ Dynamic disjunction is both internally

static and externally static.

²⁵ Not discussed here is the hybrid approach due to Kratzer 1996, where only the external argument is introduced by a distinct thematic head.

²⁶ See, e.g. Ahn 2016 and Elliott 2017 for independent evidence for this position from different domains.

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We can assume the following Logical Form (LF):

The discussion in the paper is quite confusing at this point, but Chierchia seems to assume that DR-lift extends straightforwardly to thematic argument-introducing heads. This is in fact not the case – we have to generalize DR-lift to predicates of type $e \rightarrow v \rightarrow t$.²⁷

(46) Thematic DR-lift (def.) $f^{\Delta_n} := \lambda x \cdot \lambda e \cdot \lambda \omega \omega' \cdot \omega \stackrel{n/x}{=} \omega' \wedge f x e \quad \Delta_n : (e \to v \to t) \to e \to v \to t$

We furthermore must assume that *dynamic* PM is a freely available semantic composition rule – dynamic PM is just like ordinary PM, only instead of conjoining the inner propositional value, we do dynamic sequencing.

(47) Dynamic PM (def.):
$$\begin{bmatrix} & & \\ & & \\ & & \\ & & \\ & & m_{a \to T} \end{bmatrix} := \lambda x_a \cdot m x ; n x$$

If we return to our simple example, we can now apply DR-lift every step of the

²⁷ As far as I can see, the compositional details of the system as laid out by Chierchia at this point are incoherent, but easily fixed.

way, as in figure 13:



What this essentially buys us is a sentence-internal accessibility hierarchy – the subject and object are accessible to the verb, but not nice versa, and the subject is accessible to the object, but not vice versa.

This can be leveraged in order to account for the basic cases of wco. Successful Q-binding is illustrated in figure 14; the subject is accessible to the object, so the trace of the QP comes to dynamically bind the pronoun by DR-shifting the thematic role head.

Unsuccessful Q-binding is illustrated in figure 15 – since the object is *not* accessible to the subject, discourse binding of the pronoun by the trace of the QP fails.

One thing we should be explicit about now – just how *do* quantifiers bind their traces? In the paper, it's assumed that the meta-language is something like first order logic – traces of quantifiers denote *first order* variables, and therefore as long as a trace is co-indexed with a quantifier, it is bound – traces of QPS are indirectly bound.

Chierchia therefore assumes a completely different system of indexation and binding specific to QPS. If we wanted to translate Chierchia's approach into a theory in which binding is more direct, we'd need to redefine the CCP type constructor as follows:



$(48) \quad \mathsf{T} \coloneqq \mathsf{o} \to \mathsf{o} \to \mathsf{g} \to \mathsf{t}$

The need to distinguish between first order variables and genuine pronouns has precedents in the dynamic literature²⁸, but this is arguably a conceptually unappealing aspect of the proposal.²⁹

2.6 Binding into adjuncts

Chierchia argues that, an advantage of incorporating events into the system, is that his theory straightforwardly accounts for binding into adjuncts³⁰

In event semantics, adverbials are simply interpreted as properties of events, and are incorporated into the sentence via d-PM, below existential closure.

(49) $[against John's will] = \lambda e \cdot e against will j \qquad v \to t$

Since, the adverbial is a monadic predicate, it can of course be d-lifted:

(50) [against John's will] $^{\Delta} = \lambda e \cdot \lambda \omega \omega' \cdot \omega = \omega' \wedge e$ against will j $\vee \to T$

Since adverbials are adjoined to the right typically, the system predicts that *objects are accessible to right-adjoined adverbials*. We can now account for the following example straightforwardly:

(51) John loves everyone against their will.

3 Problems

3.1 A-movement

A-movement bleeds wco:

(52) Every boy_x^1 seems to his_1 mother [t_x to be happy].

Furthermore, A-movement out of an externally static environment feeds dynamic binding:

²⁸ Dekker 1994

²⁹ See Barker & Shan's criticism of Dynamic Montague Grammar (DMG) for relevant discussion.

³⁰ At least, adverbial adjuncts that are interpreted as event modifiers – see Parsons 1990.



(53) Someone didn't leave. He sat down.

This leads to an unavoidable weakening of the DPP:

- (54) The Dynamic Predication Principle (DPP) (refined ver.) DRS can only be introduced by:
 - a. A-positions
 - b. predicates.

Theoretically, this means that the operation of DR-lifting must be licensed at derived predicates created by A-movement. This doesn't seem particularly enlightening or explanatory.

3.2 The problem of existentials

Since DR-introduction is performed by *predicates* rather than arguments, Chierchia makes a bad prediction: Scoping an indefinite out of an *externally static* environment should fail to feed binding.³¹

This is clearly a bad prediction, as illustrated by (55)

(55) It's not the case that [a certain boy $|^1$ sat down]. He₁ left hours ago.

³¹ It's not necessary to use a specific indefinite to illustrate this point, but it does make the wide-scope reading more salient.

Figure 16: Binding into adjuncts

To see *why* Chierchia makes this prediction, it's enough to consider the simple event-free fragment from the beginning.

First, consider the meaning of the prejacent of negation, with a DR-shifted predicate relative to 1. This introduces a DR corresponding to the trace of the quantifier.

(56) $[t_x \text{ sat down}] = \lambda \omega \omega'$. $\overset{1/x}{=} \omega' \wedge \text{sat-down } x$

Applying dynamic negation to the prejacent closes off the discourse referent:

1 /---

(57)
$$\neg$$
 (56) = $\lambda \omega \omega' \cdot \omega = \omega' \wedge \neg \exists \omega'' [\omega \stackrel{1/x}{=} \omega'' \wedge \text{sat-down } x]$

Now, binding the trace with an existential quantifier fails to re-introduce the DR that was wiped out by dynamic negation.

(58)
$$\exists_x (57) = \lambda \omega \omega' \cdot \omega = \omega' \wedge \exists x [\neg \exists \omega'' [\omega = \omega'' \wedge \text{sat-down } x]]$$

Chierchia concludes that (a) we should treat indefinites as *choice-functional variables*, and furthermore than (b) existential closure of a choice-functional variable introduces a DR. This is clearly a weakening of the DPP.

- (59) The Dynamic Predication Principle (DPP) (refined ver.)
 - DRS can only be introduced by:
 - a. A-positions
 - b. predicates.
 - c. existential closure of choice-functional variables.

The refined version of the theory predicts that *indefinite scope feeds DR-introduction*.

Note that this predicts that *wide-scope* indefinites should obviate wco. Chierchia argues that this is a good prediction based on the following contrasts. As has been observed before, *specific indefinites can obviate wco*.

(60) a. *His₁ father hates a boy¹.
b. ?His₁ father hates { a boy I know¹ | a certain boy¹ | a friend of mine¹ }

Unfortunately, this tying together of DR introduction and wco obviation is going to lead to a fatal flaw in Chierchia's theory. Anything that can introduce a DR by scoping out of an externally static environment must introduce a DR at its *scope site*; anything that does so is predicted to obviate wco. wh-expressions can introduce DRS:

(61) Who¹ walked in? and, did they₁ sit down?

Furthermore, *wh*-moving out of an externally static environment feed DR introduction:

(62) Who¹_x does nobody like t_x ? and, where are they₁?

Even wh-in-situ can scope out of an externally static environment, feeding DR introduction:

(63) Which $boy_y^1 t_y$ bought none of his friends which $book^2$? and, why did he₁ hate it₂ so much?

By Chierchia's logic it follows that *wh*-expressions *must* introduce DRS at their scope site, and this predicts that *wh*-scope should obviate wco. This loses one of the core cases of wco – *wh*-movement can certainly *not* obviate wco.

(64) *Which boy¹_x does his₁ father hate t_x ?

(65) *Which book¹_x did John give none of it₁s fans t_x ?

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