

A Flexible Scope Theory of Intensionality*

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1 Roadmap

- Fact: predicates are *world-sensitive*; in an intensional context, DPs may be interpreted *de re* or *de dicto*:

- (1) George wants $\overbrace{[\text{the Red Sox players}]}$ to win the game].
- DE RE: interpretation, *Red Sox player* is interpreted relative to the utterance evaluation world.
 - DE DICTO: *Red Sox player* is interpreted relative to George's *want*-worlds.

- Two broad camps in accounting for world sensitivity – the Binding Theory of Intensionality (BTI)¹ and the Scope Theory of Intensionality (STI).²
- The BTI is powerful, but must be supplemented with a binding theory for world variables. The STI is much more restrictive, but (seemingly) under-generates.

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¹Percus (2000), Heim & von Fintel (2011: chapter 8), etc.

²Heim & von Fintel (2011) call this the *standard theory*.

- Scope theory state of the art – Keshet's *split intensionality*³ – succeeds in addressing some of the worst over-generation issues, but others remain.
- Concretely, Grano (2019) shows that the account of exceptional *de re* for indefinites runs into insurmountable obstacles.
- I'll aim to improve on split intensionality by presenting a new take on the STI – which I'll call the *flexible scope theory* – whereby expressions can receive exceptional *de re* interpretations via recursive scope-taking, facilitated by a minimal inventory of type-shifters.
- The flexible scope theory will preserve a central claim of split intensionality – *de re* requires movement to an edge position.
- The resulting theory will bear a (non-accidental) family resemblance to Charlow's (2014, 2019) theory of exceptionally-scoping indefinites.

2 Split intensionality

- The scope theory says, roughly, that an expression is interpreted *de dicto* if it scopes below an intensional operator, and *de re* if it scopes above an intensional operator.
- One immediate problem for the scope theory is the fact that scope islands do not always block *de re* interpretations.⁴

- (3) George thinks $\overbrace{[\text{every Red Sox player}]}$ is staying in the Ritz-Carlton].

- Keshet's *split intensionality* theory is tailored to circumvent this problem.
- Keshet assumes that embedded clauses basically denote extensions, and attitude verbs are looking for intensions – in order to repair this mismatch, a type-shifter \wedge is inserted at the clause-edge.

³Keshet 2008, 2011

⁴This is of course no problem for the BTI, assuming free insertion of an abstraction index at the edge of the matrix clause.

- (2) 1 George thinks every Red Sox player_{w1} is staying in the Ritz Carlton.

- A QP may be interpreted *de re*, while nevertheless receiving narrow quantificational scope, by QR-ing to a position above $\hat{\ }$ but below the attitude verb.

(4) George thinks every Red Sox player $\lambda x \hat{\ }$ [t_x is staying in the Ritz-Carlton].

- In effect, $\hat{\ }$ serves to create a privileged position at the clause edge in which QPs can be exceptionally interpreted *de re*.

2.1 Problem 1: doubly-embedded *de re*

- We can note already that a straightforward prediction of split intensionality is that an expression can only be interpreted *de re* relative to the *minimally* containing scope island.
- At face value, it is clear that this generalization doesn't hold, as pointed out by Grano. Consider the following example from Grano (2019: p. 162):

(5) a. *There is a group of people in this room. Neither Jo nor Mary know that they're in this room. Mary hopes they're actually outside. She reports her hope to Jo, and Jo believes her.*
 b. ✓ Jo thinks [that Mary hopes [that everyone in this room is outside]].

- So, it seems like there are simple cases in which split intensionality isn't sufficiently general.⁵

⁵Of course, this isn't accidental, but rather a design feature of Keshet's analysis. In support of this, Keshet observes (a) that counterfactuals with tautologous antecedents sound odd, and (b) if exceptional *de re* were available, it should rescue embedded counterfactuals.

- (6) #If three professors were professors, the classes would be better taught.
 (7) #Mary thinks that if three professors were professors, the classes would be better taught.

I don't have much to say about these examples, except that they can be much improved with some manipulation.

- (8) a. #If three syntacticians were linguists, the classes would be more fun.
 b. Mary thinks that the classes would be better taught if three syntacticians were linguists – she has no idea what they do!

2.2 Problem 2: Bäuerle's puzzle

- Consider the following example:⁶

(9) George thinks every Red Sox player is staying in some five star hotel downtown.

- There is a reading with the following features:
 - *Red Sox player* is interpreted *de re* – George's beliefs pertain to a group of men who happen to be Red Sox players, potentially unbeknownst to George.
 - *Five star hotel* is interpreted *de dicto* – George's beliefs involve a five star hotel; the sentence may still be true even if there are no five star hotels, just so long as George believes that there are.
 - *Some* takes scope over *every* – George thinks that all the people in question are staying at the *same* five star hotel downtown.
- If we take any version of the STI, such as split intensionality, this reading would seem to place contradictory requirements on the scope of *some five star hotel*.
 - In order for *some five star hotel* to be interpreted *de dicto*, it should scope below $\hat{\ }$.

(10) $\hat{\ } >$ some fsh

- In order for *every Red Sox player* to be interpreted *de re*, it should scope above $\hat{\ }$.

(11) every rsp $>$ $\hat{\ }$

- By transitivity, this means that *every Red Sox player* should have to take scope over *some five star hotel* – but this doesn't capture the reading we're interested in. Whoops!

- Keshet (2010) suggests that *some five star hotel* is a *specific indefinite*, and therefore involves a choice-functional variable existentially bound.⁷

⁶From Keshet 2010: p. 692, ex 1, loosely based on an example in German from Bäuerle (1983).

⁷A function f is a *choice function* iff f is of type $(a \rightarrow t) \rightarrow a$, and for any predicate P , $f P \in P$

- Keshet’s innovation is the suggestion that the choice function returns a member of the NP restrictor at the local evaluation world.
- Together with the *split intensionality hypothesis*, this allows him to derive the problematic reading with the following LF:

(12) $\exists f$ George thinks every Red Sox player $\lambda x \wedge [x$ is staying in f (five star hotel)].

As demonstrated by Grano (2019), exceptionally-scoping indefinites can also receive *de re* interpretations.⁸

(13) a. *Jo and Bill are out shopping. Bill finds a hat that he likes and considers purchasing it. It so happens that the hat is just like mine, but neither Jo nor Bill know this. Jo thinks that that the hat looks great on Bill and hopes he’ll buy it.*

b. ✓ Jo hopes [that Bill will buy a hat just like mine].

- Keshet can account for this by QRing the restrictor of the indefinite to a position above the intensionalizing operator at the edge of the scope island.

(14) $\exists f$ Jo hopes f (hat just like mine) $\lambda x \wedge [$ Bill will buy $t_x]$

- This solution seems to work just fine, but as pointed out by Grano 2019, it won’t generalize to cases involving more deeply embedded scope islands.⁹

(15) a. *Mary, Jo, and Bill are out shopping. Bill finds a hat that he likes and considers purchasing it. It so happens that the hat is just like mine, but neither Mary, nor Jo, nor Bill know this. Jo thinks that the hat looks great on Bill and hopes he’ll buy it. Jo expresses her hope out loud, and Mary believes Jo.*

b. Mary thinks [that Jo hopes [that Bill will buy a hat just like mine]].

- Since QR is clause-bounded, the best Keshet can do is the following LF, which doesn’t derive the attested reading:

(16) $\exists f$ Mary thinks that Jo hopes [a hat just like mine] $\lambda x \wedge [$ Bill will buy $t_x]$.

⁸The following example from Grano 2019: p. 162.

⁹The following example from Grano 2019: p. 162.

- In the remainder of the paper, Grano (2019) briefly lays out (and rejects) other possible moves Keshet could make. I won’t dwell on the remainder of the argumentation here, but I’ll take this as a prompt to try to do better.

3 Scope theory *redux*

- In this section, we’ll start from minimal means and bootstrap a different way of achieving world-sensitivity that (I’ll argue) slices the pie in just the right way.

- I’ll assume that predicates deliver propositions rather than truth values, i.e.,¹⁰

(18) $\llbracket \text{swim} \rrbracket := \lambda x w . \text{swim}_w x \quad e \rightarrow S t$

- Without going into the details of DP-internal composition (yet), I’ll assume without argument that definite descriptions denote *individual concepts*, i.e., world-sensitive individuals.

(19) $\llbracket \text{the boy} \rrbracket = \lambda w . \iota x [\text{boy}_w x] \quad S e$

- Thinking through the problem of how to compose (19) with (18) will be the key to unlocking an intensional grammar with just the combinatoric potential we need to achieve *exceptional de re*.

- Below, I define a composition rule \star (pronounced: *bind*) in order to accomplish just this.¹¹¹²

(20) Bind (def.)
 $m^\star := \lambda k . \lambda w . (k (m w)) w \quad \star : S a \rightarrow (a \rightarrow S b) \rightarrow S b$

¹⁰Here, S is the *type constructor* for world-sensitive values.

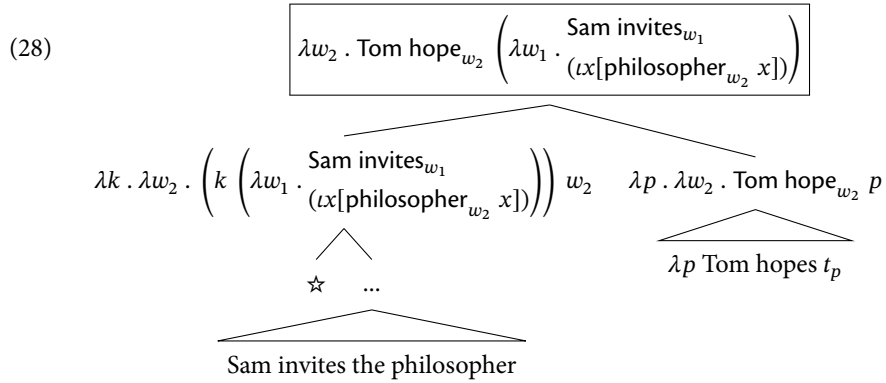
(17) $S a := s \rightarrow a$
 In other words, its a function from types to intensional types. Here, s is the type of worlds.

¹¹If you’re familiar with haskell (or category theory), you’ll recognize the type signature of bind. Where m is a monad, monadic bind is of type $m a \rightarrow (a \rightarrow m b) \rightarrow m b$

In fact, our bind is just the bind of a Reader monad.

¹²N.b. that, for our purposes, we could have made bind rigidly typed, where $a = e$, and $b = t$. Instead, I’ve given bind a maximally polymorphic type based on what we want it to do.

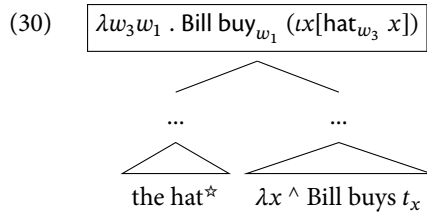
- STEP 2: Bind-shift the scope island, and QR it to the edge of the matrix clause. (31)



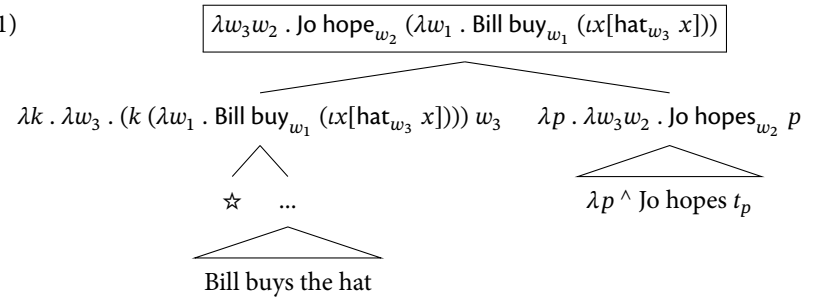
- We've successfully derived the *de re* reading of the definite. This mechanism is recursive, and will therefore generalize to more deeply embedded scope islands:

(29) Mary thinks [that Jo hopes [that Bill buys the hat just like mine]].

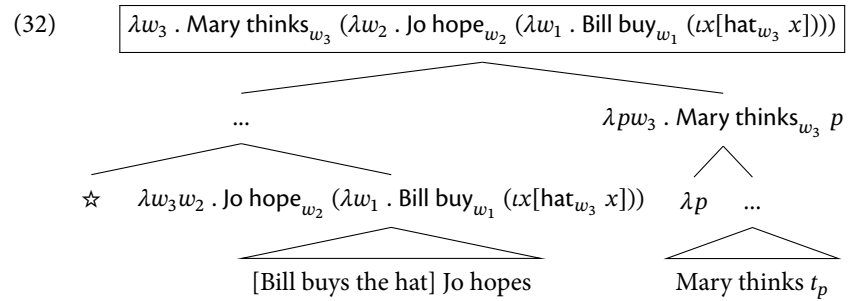
- STEP 1: scope the definite over an up-shifter:



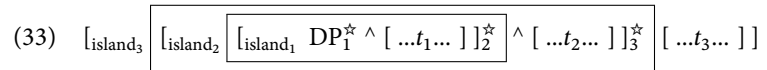
- STEP 2: bind-shift the scope island and scope it over an up-shifter:



- STEP 3: bind-shift the result, and scope it to the edge of the matrix clause:



- Schematically, a *de re* interpretation for a DP embedded in two scope islands can be derived via the following LF:



- An intermediate *de re* interpretation can be derived by only scoping the inner-most scope island.
- The mechanism for deriving exceptional *de re* therefore, at LF, involves *cyclic*

scope-taking (Charlow 2019).^{13,14}

3.2 Evidence for scope

- Since Keshet (2011), for independent reasons, rejects a scope-based theory of *de re* interpretations on definites, it's worth dwelling on what this buys us.
- Romoli & Sudo observe a constraint on *de re/de dicto* readings of nested DPs:

(34) *Nested DP constraint*

When a DP is embedded inside a DP, the embedding DP must be opaque if the embedded DP is opaque.

- If we take the following sentence, this blocks a reading where *president* takes narrow intensional scope, and *wife* takes (exceptionally) wide intensional scope:

(35) Mary thinks the wife of the president is nice.

- As Romoli & Sudo (2009) observe, the sentence is intuitively false in the following context: *Mary sees Bono Vox on TV with his wife Alison Hewson. Mary wrongly believes that he is the president, and furthermore, that the nice woman next to him is his sister. Thus, the wife-relation is actually true, but the characterization of Bono Vox as the president is not*
- On the vTI , this reading is easy to generate. On a scope theory however, such as the one outlined here, the corresponding LF will inevitably involve an unbound trace (here: t_3):

(36) * [island [the wife of t_3] $_2^*$ ^ [the president] $_3^*$ t_2 is nice] $_1^*$ Mary thinks t_3 .

¹³It's not a coincidence that the combinatorics for exceptional *de re* bear a resemblance to Charlow's (2019) account of exceptionally-scoping indefinites via cyclic scope.

The type-constructor S , alongside the bind-shifter and up-shifter constitute a typed instantiation of the Reader monad.

Charlow shows in detail how the bind associated with a given monad M can be interpreted as a method for lifting a value of type $M a$ into a scope-taker.

¹⁴I've framed the analysis here in terms of quantifier raising, but a completely isomorphic could be given in a fragment which uses *continuations* (Barker 2002, Barker & Shan 2014) as an in-situ scope-taking mechanism, as in Charlow 2014. It's hard to find genuinely *syntactic* evidence for the movements posited here, so ultimately this may be a better way to go.

4 Towards an account of Bäuerle's puzzle

4.1 Extending the fragment

- There are (at least) two outstanding issues with the current state of our fragment:
 - We haven't said anything yet about DP-internal composition.
 - We haven't said anything yet about what QPs denote, so we aren't in a position to address Grano's challenge.

- It will turn out that resolving the former issue will also give us a natural answer to the latter.
- Let's begin by thinking about how a definite determiner composes with its restrictor.

(37) $\llbracket \text{the} \rrbracket := \lambda R . \iota x [R x] \quad (e \rightarrow t) \rightarrow e$

- If we want our rule to be maximally general, we need a way of composing something of type $S ((a \rightarrow b) \rightarrow c)$ with something of type $a \rightarrow S b$ to give back something of type $S c$.
- We'll accomplish via a new operation, which we'll call *c-lift*. *C-lift* captures a similar intuition to *bind* – *bind* provides a way of lifting intensional values into intensional scope-takers; *c-lift* provides a way of lifting intensional scope-takers into scope-takers with an intensional return type.¹⁵

(40) *C-lift* (def.)
 $m^* := \lambda n w . m w (\lambda x . n x w) \quad S ((a \rightarrow b) \rightarrow c) \rightarrow (a \rightarrow S b) \rightarrow S c$

¹⁵For the Haskellers/category theorists in the audience, you'll notice that, although extremely useful for lifting natural language determiners, this is not a very familiar type-signature. In fact, this is operation requires something strictly stronger than a monad, namely a monad m for which an operation *inject* can be defined:

(38) $\text{inject} : (a \rightarrow m b) \rightarrow m (a \rightarrow b)$
As far as I can tell, a "natural" implementation of *inject* should be subject to the following identity law:

(39) $\lambda f . \lambda x . f \text{map} (\lambda k . k x) (\text{inject } f) = id$

- Once we up-shift our determiner, we can c-lift it to achieve the following result – a function from a restrictor to an individual concept of type $(e \rightarrow S t) \rightarrow S e$. (47)
 - $\llbracket \text{every Red Sox player} \rrbracket = \lambda w k . \forall y [\text{rsp}_w y \rightarrow k y]$
 - $\llbracket \text{some five star hotel} \rrbracket = \lambda w k . \exists x [\text{fsh}_w x \wedge k x]$

(41) $(\wedge \llbracket \text{the} \rrbracket)^* = \lambda n w . \iota x [n x w]$ $(e \rightarrow S t) \rightarrow S e$

- Exactly the same trick will generalize to the quantificational determiners.

(42) $\llbracket \text{every} \rrbracket := \lambda r s . \forall x [r x \rightarrow s x]$ $(e \rightarrow t) \rightarrow t$

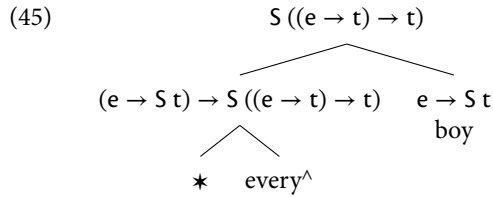
- If we first up-shift it, and then c-lift the result, we get the following meaning; a function from a predicate to an intensional scope-taker:

(43) $\llbracket \text{every} \rrbracket^{*\circ\wedge} = \lambda r w . \lambda s . \forall x [r x w \rightarrow s x]$ $(e \rightarrow S t) \rightarrow S ((e \rightarrow t) \rightarrow t)$

- Composing this meaning with a restrictor, e.g., *boy*, will result in the following:

(44) $\lambda w . \lambda s . \forall x [\text{boy}_w x \rightarrow s x]$ $S ((e \rightarrow t) \rightarrow t)$

- The internal composition for a QP therefore follows from the following LF:



4.2 Back to Bäuerle’s puzzle

- We now have all the pieces we need to account for Bäuerle’s puzzle.

(46) George thinks every Red Sox player is staying in some five star hotel downtown.

- I’ll assume that the meanings of *every Red Sox player* and *some five star hotel* are assembled via c-lift:

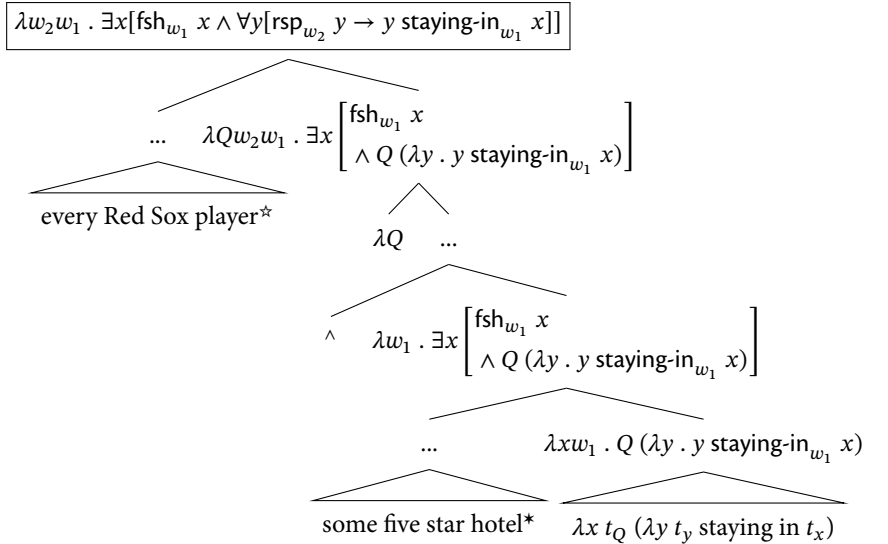
- if we take an intensional QP, and c-lift it *again*, we derive something that scopes at an intensional abstract:

(48) $\llbracket \text{every Red Sox player} \rrbracket^* = \lambda k . \lambda w . \forall y [\text{rsp}_w y \rightarrow k y w]$

- Inside of the embedded clause, *some five star hotel* scopes to a position below the *up* operator, via c-lift.

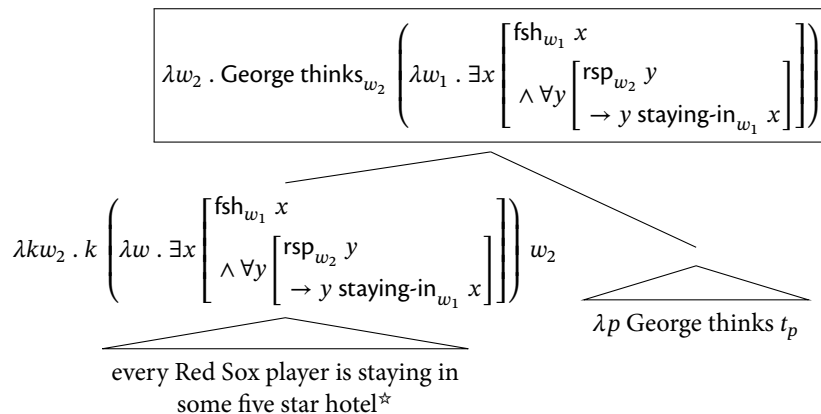
- every Red Sox player* scope to a position *above* the up-shifter via bind, leaving behind a higher-type trace below the existential’s scope site.¹⁶

(49) STEP 1: compute the value of the embedded clause



¹⁶In this upgraded fragment, bind is still essential in order to allow for semantic reconstruction.

(50) STEP 2: scope the embedded clause out via bind



5 Specificity and transparency

- More generally, this system divorces intensionality and quantification in a systematic way. Consider the famous constellation of readings for the following sentence, as discussed by Fodor (1970).

(51) Mary wants to buy an expensive coat.

a. ✓ Non-specific opaque

Narrow quantificational and intensional scope

b. ✓ Specific transparent

Wide quantificational and intensional scope

c. ✓ Non-specific transparent

Narrow quantificational and wide intensional scope

d. ✗ Specific opaque

Wide quantificational and narrow intensional scope

5.1 Non-specific opaque

- This is easy – an c-lifted QP scopes below *want*.

(52) Mary wants [an expensive coat* (λx PRO buy t_x)]

- Quantificational and intensional effects scope together.

5.2 Specific transparent

- This is easy too – an c-lifted QP scopes above *want*.

(53) [an expensive coat* (λx Mary wants PRO buy t_x)].

- Quantificational and intensional effects scope together.

5.3 Non-specific transparent

- There are at least two ways we could achieve this:
- (i) A bind-shifted QP scopes above *want*, and the quantificational part of the meaning reconstructs:¹⁷

(54) [an expensive coat* (λQ Mary wants (Q (λx PRO buy x)))].

- (ii) A c-lifted QP scopes to the edge of the embedded infinitival over an up-shifter, which in-turn is bind-shifted and scopes above *want*.¹⁸

(56) [an expensive coat* λx ^ PRO buy x (λp Mary wants p)].

- Intensional effects can out-scope quantificational effects.

5.4 Specific opaque

- There is no obvious way of achieving wide quantificational and narrow intensional scope on this system.

¹⁷Achieving the so-called “third reading” via semantic reconstruction was proposed in Heim & von Stechow 2011: chapter 8.2.7.

¹⁸There’s no motivation for positing pied-piping in this particular case since the complement of *want* isn’t a scope island.

(55) A different student wants to attend every seminar.

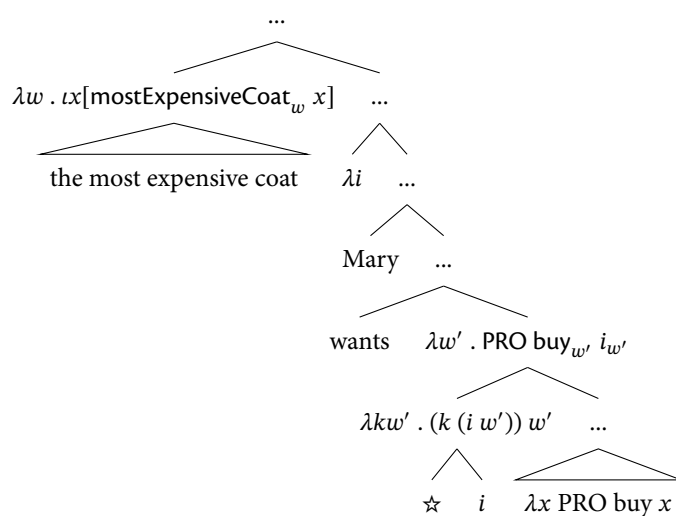
∨ > ∃

- One possibility we could entertain is that certain expressions can leave behind a type $S e$. This allows, e.g., definite descriptions to *totally semantically reconstruct*.
- Consider, e.g., the following example:

(57) The most expensive coat, MARY wants to buy.

- *The most expensive coat* can be interpreted *de dicto*. In order to account for this, we can totally semantically reconstruct the definite description.¹⁹

(58)



- However, based on the machinery we’ve introduced for lifting classical GQs into intensional operators, determiners always induce quantification over (extensional) individuals.
- Since we derive meanings for QPs of type $S((e \rightarrow t) \rightarrow t)$, then if they can leave behind traces of this same type, we predict that QPs should be able to totally reconstruct too. This seems right:

(59) An expensive coat, Mary wants to buy.

- Based on the machinery we’ve introduced however, there’s no way to derive a quantifier over individual concepts from a classical GQ. Intuitively, this is what we would need to derive narrow intensional scope and wide quantificational scope.
- CONJECTURE: there are no natural language quantifiers which quantify over individual concepts.

6 Conclusion

- Starting from the assumption that definite descriptions denote individual concepts, and predicates return propositions, we’ve shown the following:
 - A natural operation that shifts a description into a scope-taker (\star), alongside an operation for deriving trivially intensional meanings (\wedge) *automatically* gives rise to exceptional *de re*; this is because, much like definite descriptions, scope islands can be bind-shifted.
 - A natural operation for shifting determiners (\star), automatically gives rise to a system in which quantificational and intensional scope are divorced – either quantificational and intensional effects scope together, or intensional effects outscope quantificational effects (the third reading).
- The result is a *flexible* scope theory which inherits many of the advantages of classical scope theory (Romoli & Sudo’s generalization, etc.), while avoiding under-generation pitfalls (exceptional *de re*, Bäuerle’s puzzle, etc.).
- *World-sensitivity* slots neatly into a broader family of “effects” that may take exceptional scope via recursive scope taking.

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¹⁹Technically, the QP semantically reconstructs to an intermediate position, where it is bind-shifted.

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